# Type-based XML processing in Logic Programming 

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14 January, 2003

## Motivation

- XML: Standard for information exchange.


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- XSLT, DOM and SAX.


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- Static validation.


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- XML: Standard for information exchange.
- XSLT, DOM and SAX.
- Static validation.
- XDuce and HaXml .


## Main Goal

Use of Logic Programming with static validation for XML processing.

## Implementation

1. Translator from XML to Prolog.

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2. Translator from DTDs to Regular Types.

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2. Translator from DTDs to Regular Types.
3. Type inference.

## Implementation

1. Translator from XML to Prolog.
2. Translator from DTDs to Regular Types.
3. Type inference.
4. Translator from Prolog to XML.

## Outline

XML

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- XML
- DTD


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- DTD
- Translation from XML to Prolog


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- Translation from DTDs to Regular Types
- Type inference for XML processing programs


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- Type inference (Zobel 1990)
- Translation from DTDs to Regular Types
- Type inference for XML processing programs
- Conclusions


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- Type inference for XML processing programs
- Conclusions
- Future Work


## XML - eXtensible Markup Language

## XML - eXtensible Markup Language

## Example:

```
<addressbook>
    <name>Jorge</name>
    <address>Porto</address>
    <email>jorge@mailserver.pt</email>
    <name>Mario</name>
    <address>Lisboa</address>
    <address>Portugal</address>
    <phone>
        <home>12457834</home>
    </phone>
</addressbook>
```


## Document Type Definition

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DTDs are grammars that specify the document structure.

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DTDs are grammars that specify the document structure.

## Example:

<!ELEMENT addressbook (name,address+,phone?,email?)*>
<!ELEMENT name (\#PCDATA)>
<!ELEMENT address (\#PCDATA)>
<!ELEMENT phone (home,mobile*)>
<!ELEMENT email (\#PCDATA)>
<!ELEMENT home (\#PCDATA)>
<!ELEMENT mobile (\#PCDATA)>

## Translation from XML to Prolog

## Translation from XML to Prolog

## Element with only character data

$$
\begin{aligned}
& \text { <!ELEMENT b (\#PCDATA)> } \\
& \text { <b>Text of element } b</ \mathrm{b}> \\
& \mathrm{b}(\text { "Text of element } \mathrm{b} ")
\end{aligned}
$$

## Translation from XML to Prolog

## Element with only character data

<!ELEMENT b (\#PCDATA)><br><b>Text of element b</b><br>b("Text of element b")

## Empty element

<!ELEMENT b EMPTY>
<b/>
b

## Translation from XML to Prolog

## Element with sub elements

> <!ELEMENT a (b, c)>
> <!ELEMENT b (\#PCDATA)>
> <!ELEMENT c (\#PCDATA)>

```
<a>
    <b> Text for element b </b>
    <c> Text for element c </c>
</a>
a(
    b(" Text for element b "),
    c(" Text for element c "))
```


## Translation from XML to Prolog

## Element with zero or more occurrences

$$
\begin{aligned}
& \text { <!ELEMENT a (b)*> } \\
& \text { <!ELEMENT b (\#PCDATA)> } \\
& \text { <a> } \\
& \text { <b> First b </b> } \\
& \text { <b> Second b </b> } \\
& \text { <b> Third b </b> } \\
& \text { </a> } \\
& \text { a( } \\
& \text { [b(" First b "), } \\
& \text { b(" Second b "), } \\
& \text { b(" Third b ")]) }
\end{aligned}
$$

## Translation from XML to Prolog

Element with one or more occurrences

```
<!ELEMENT a (b+,c)>
<!ELEMENT b (#PCDATA)>
<!ELEMENT c (#PCDATA)>
<a>
    <b> Text for b </b>
    <c> Text for c </c>
</a>
al
    [b(" Text for b ")],
    c(" Text for c "))
```


## Translation from XML to Prolog

## Optional element



## Translation from XML to Prolog

Disjoint elements

$$
\begin{gathered}
\text { <!ELEMENT a (b|c)> } \\
\text { <!ELEMENT b (\#PCDATA)> } \\
\text { <!ELEMENT c (\#PCDATA)> } \\
\text { <a> <b> Text </b> </a> } \\
\text { <a> <c> Another text </c> </a> } \\
\text { a(b(" Text ")) } \\
\text { a(c(" Another text ")) }
\end{gathered}
$$

## Translation guided by DTDs

Using two distinct DTDs to validate the same document can lead to different (valid) terms:

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Using two distinct DTDs to validate the same document can lead to different (valid) terms:
<b> First b </b>
<b> Second b </b>

```
    <!ELEMENT a b*>
    <!ELEMENT b (#PCDATA)>
a(
    [b(" First b "),
    b(" Second b ")])
```

$$
\begin{aligned}
& \text { <a> } \\
& \text { </a> } \\
& \text { <! ELEMENT a (b,b)> } \\
& \text { <!ELEMENT b (\#PCDATA)> } \\
& \text { al } \\
& \text { b(" First b "), } \\
& \text { b(" Second b ")) }
\end{aligned}
$$

## Regular Types

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Regular types are defined as the class of types that can be specified by sets of type rules.

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Type symbol

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Given the following rules:

- $\alpha \rightarrow\{a\}$
- $\beta \rightarrow\{$ nil, . $(\alpha, \beta)\}$


## Regular Types

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\underbrace{\text { Type symbol } \rightarrow \text { Types that describe terms }\}}_{\text {Type Rule }}
$$

Given the following rules:

- $\alpha \rightarrow\{a\}$
- $\beta \rightarrow\{$ nil, . $(\alpha, \beta)\}$

Regular Types produced by $\alpha$ :
$\{a\}$

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$\{a\}$

## Regular Types produced by $\beta$ :

$$
\{n i l, .(a, n i l), .(a, a, n i l), \ldots\}
$$

## Type inference (Zobel 1990)

We built a type inference system that uses Regular Types as an approximation to program types. For example, given the next program:

```
p(0).
p(f(X)):-q(X),X=f(Y).
q(f(0)).
q(g(X)).
q(f(X)):-p(X).
```


## Type inference (Zobel 1990)

We built a type inference system that uses Regular Types as an approximation to program types. For example, given the next program:

The system reaches the following types:

- $\alpha_{p} \rightarrow\left\{0, f\left(f\left(\alpha_{1}\right)\right)\right\}$
- $\alpha_{q} \rightarrow\left\{g(\mu), f\left(\alpha_{1}\right)\right\}$
- $\alpha_{1} \rightarrow\left\{0, \alpha_{p}\right\}$


## Translating from DTDs to Regular Types

## Translating from DTDs to Regular Types

Element with only character data

$$
\mathcal{T}(<!\text { ELEMENT } e(\text { \#PCDATA })>)=\tau_{e} \rightarrow\{e(\text { string })\}
$$

## Translating from DTDs to Regular Types

Element with only character data
$\mathcal{T}(<!$ ELEMENT $e(\#$ PCDATA $)>)=\tau_{e} \rightarrow\{e($ string $)\}$
<!ELEMENT a (\#PCDATA) >

## Translating from DTDs to Regular Types

Element with only character data
$\mathcal{T}(<!$ ELEMENT $e($ \#PCDATA $)>)=\tau_{e} \rightarrow\{e($ string $)\}$
<!ELEMENT a (\#PCDATA)>

$$
\tau \rightarrow\{a(\text { string })\}
$$

## Translating from DTDs to Regular Types

## Empty element

$$
\mathcal{T}(<!\text { ELEMENT } e \text { EMPTY }>)=\tau_{e} \rightarrow\{e\}
$$

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<!ELEMENT a EMPTY>

## Translating from DTDs to Regular Types

## Empty element

$$
\mathcal{T}(<!\text { ELEMENT } e \text { EMPTY }>)=\tau_{e} \rightarrow\{e\}
$$

<!ELEMENT a EMPTY>

$$
\tau \rightarrow\{a\}
$$

## Translating from DTDs to Regular Types

Element with any contents

$$
\mathcal{T}(<!\text { ELEMENT } e \text { ANY }>)=\tau_{e} \rightarrow\{e(\mu)\}
$$

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Element with any contents

$$
\mathcal{T}(<!\text { ELEMENT } e \text { ANY }>)=\tau_{e} \rightarrow\{e(\mu)\}
$$

<!ELEMENT a ANY>

## Translating from DTDs to Regular Types

Element with any contents

$$
\mathcal{T}(<!\text { ELEMENT } e \text { ANY }>)=\tau_{e} \rightarrow\{e(\mu)\}
$$

<!ELEMENT a ANY>

$$
\tau \rightarrow\{a(\mu)\}
$$

## Translating from DTDs to Regular Types

## Element with sub elements

$\mathcal{T}\left(<!E L E M E N T e\left(e_{1}, \ldots, e_{n}\right)>=\tau_{e} \rightarrow\left\{e\left(\tau_{e_{1}}, \ldots, \tau_{e_{n}}\right)\right\}\right.$, where
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{i}>\right)=\tau_{e_{i}} \rightarrow \Upsilon_{e_{i}}$, for $1 \leq i \leq n$

## Translating from DTDs to Regular Types

## Element with sub elements

$\mathcal{T}\left(<!\right.$ ELEMENT $e\left(e_{1}, \ldots, e_{n}\right)>=\tau_{e} \rightarrow\left\{e\left(\tau_{e_{1}}, \ldots, \tau_{e_{n}}\right)\right\}$, where
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{i}>\right)=\tau_{e_{i}} \rightarrow \Upsilon_{e_{i}}$, for $1 \leq i \leq n$
<!ELEMENT a (b, c) >
<!ELEMENT b (\#PCDATA)>
<!ELEMENT c (\#PCDATA)>

## Translating from DTDs to Regular Types

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$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{i}>\right)=\tau_{e_{i}} \rightarrow \Upsilon_{e_{i}}$, for $1 \leq i \leq n$
<!ELEMENT a (b, c) >
<!ELEMENT b (\#PCDATA) >
<!ELEMENT c (\#PCDATA)>

$$
\begin{array}{lll}
\tau_{1} & \rightarrow\left\{a\left(\tau_{2}, \tau_{3}\right)\right\} \\
\tau_{2} & \rightarrow\{b(\text { string })\} \\
\tau_{3} & \rightarrow & \{c(\text { string })\}
\end{array}
$$

## Translating from DTDs to Regular Types

## Element with zero or more occurrences

$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e e_{1} *>\right)=\tau_{e} \rightarrow\left\{\right.$ nil,. $\left.\left(\tau_{e_{1}}, \tau_{e}\right)\right\}$, where
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{1}>\right)=\tau_{e_{1}} \rightarrow \Upsilon_{e_{1}}$

## Translating from DTDs to Regular Types

## Element with zero or more occurrences

$$
\begin{aligned}
\mathcal{T}\left(<!\text { ELEMENT } e e_{1} *>\right)= & \tau_{e} \rightarrow\left\{\text { nill,. }\left(\tau_{e_{1}}, \tau_{e}\right)\right\}, \text { where } \\
& \mathcal{T}\left(<!\text { ELEMENT } e_{1}>\right)=\tau_{e_{1}} \rightarrow \Upsilon_{e_{1}}>
\end{aligned}
$$

<!ELEMENT a b*>
<!ELEMENT b (\#PCDATA)>

## Translating from DTDs to Regular Types

## Element with zero or more occurrences

$\mathcal{T}\left(<!\right.$ ELEMENT e $\left.e_{1} *>\right)=\tau_{e} \rightarrow\left\{\right.$ nil,. $\left.\left(\tau_{e_{1}}, \tau_{e}\right)\right\}$, where
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{1}>\right)=\tau_{e_{1}} \rightarrow \Upsilon_{e_{1}}$
<!ELEMENT a b*>
<!ELEMENT b (\#PCDATA)>

$$
\begin{aligned}
\tau_{1} & \rightarrow\left\{a\left(\tau_{2}\right)\right\} \\
\tau_{2} & \rightarrow\left\{\text { nil, } .\left(\tau_{3}, \tau_{2}\right)\right\} \\
\tau_{3} & \rightarrow\{b(\text { string })\}
\end{aligned}
$$

## Translating from DTDs to Regular Types

Element with one or more occurrences

$$
\begin{aligned}
\mathcal{T}\left(<!\text { ELEMENT } \text { e } e_{1}+>\right)= & \tau_{e} \rightarrow\left\{.\left(\tau_{e_{1}}, \text { nil }\right) . .\left(\tau_{e_{1}}, \tau_{e}\right)\right\} \text {, where } \\
& \mathcal{T}\left(<!\text { ELEMENT } e_{1}>\right)=\tau_{e_{1}} \rightarrow \Upsilon_{e_{1}}
\end{aligned}
$$

## Translating from DTDs to Regular Types

Element with one or more occurrences

$$
\begin{aligned}
\mathcal{T}\left(<!\text { ELEMENT } \text { e } e_{1}+>\right)= & \tau_{e} \rightarrow\left\{.\left(\tau_{e_{1}}, \text { nil }\right) . .\left(\tau_{e_{1}}, \tau_{e}\right)\right\} \text {, where } \\
& \mathcal{T}\left(<!\text { ELEMENT } e_{1}>\right)=\tau_{e_{1}} \rightarrow \Upsilon_{e_{1}}
\end{aligned}
$$

<!ELEMENT a b+>
<!ELEMENT b (\#PCDATA)>

## Translating from DTDs to Regular Types

Element with one or more occurrences
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e e_{1}+>\right)=\tau_{e} \rightarrow\left\{.\left(\tau_{e_{1}}\right.\right.$, nil $\left.), .\left(\tau_{e_{1}}, \tau_{e}\right)\right\}$, where $\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{1}>\right)=\tau_{e_{1}} \rightarrow \Upsilon_{e_{1}}$
<!ELEMENT a b+>
<!ELEMENT b (\#PCDATA)>

$$
\begin{aligned}
\tau_{1} & \rightarrow\left\{a\left(\tau_{2}\right)\right\} \\
\tau_{2} & \rightarrow\left\{\cdot\left(\tau_{3}, \text { nil }\right), .\left(\tau_{3}, \tau_{2}\right)\right\} \\
\tau_{3} & \rightarrow\{b(\text { string })\}
\end{aligned}
$$

## Translating from DTDs to Regular Types

Disjoint elements
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e\left(e_{1}|\cdots| e_{n}\right)>\right)=\tau_{e} \rightarrow\left\{\tau_{e_{1}}, \ldots, \tau_{e_{n}}\right\}$, where
$\mathcal{T}\left(<!\right.$ ELEMENT $\left.e_{i}>\right)=\tau_{e_{i}} \rightarrow \Upsilon_{e_{i}}$, for $1 \leq i \leq n$
<!ELEMENT a (b|c)>
<!ELEMENT b (\#PCDATA)>
<!ELEMENT c (\#PCDATA)>
<!ELEMENT a (b|c)>
<!ELEMENT b (\#PCDATA)>
<!ELEMENT c (\#PCDATA)>

$$
\begin{aligned}
\tau_{1} & \rightarrow\left\{a\left(\tau_{2}\right)\right\} \\
\tau_{2} & \rightarrow\left\{\tau_{3}, \tau_{4}\right\} \\
\tau_{3} & \rightarrow\{b(\text { string })\} \\
\tau_{4} & \rightarrow\{c(\text { string })\}
\end{aligned}
$$

## Translating from DTDs to Regular Types

## Optional element

$$
\begin{aligned}
\mathcal{T}\left(<!\text { ELEMENT } e\left(e_{1}, \ldots, e_{i} ?, \ldots, e_{n}\right)\right) & =\tau_{e} \rightarrow\left\{e\left(\tau_{e_{1}}, \ldots, \tau_{e_{i-1}}, \tau_{e_{i+1}}, \ldots, \tau_{e_{n}}\right),\right. \\
& \left.e\left(\tau_{e_{1}}, \ldots, \tau_{e_{i-1}}, \tau_{e_{i}}, \tau_{e_{i+1}}, \ldots, \tau_{e_{n}}\right)\right\}, \\
& \text { where } \\
& \mathcal{T}\left(<!\text { ELEMENT } e_{i}>\right)=\tau_{e_{i}} \rightarrow \Upsilon_{e_{i}}, \\
& \text { for } 1 \leq i \leq n
\end{aligned}
$$

## Translating from DTDs to Regular Types

Optional element

<!ELEMENT a (b,c?,d?)>
<!ELEMENT b (\#PCDATA)>
<!ELEMENT c (\#PCDATA)>
<!ELEMENT d (\#PCDATA)>

## Translating from DTDs to Regular Types

## Optional element

> <!ELEMENT a (b,c?,d?)> <!ELEMENT b (\#PCDATA)> <! ELEMENT c (\#PCDATA)> <!ELEMENT d (\#PCDATA)>

$$
\begin{aligned}
\tau_{1} \rightarrow & \left\{a\left(\tau_{2}\right), a\left(\tau_{2}, \tau_{3}\right),\right. \\
& \left.a\left(\tau_{2}, \tau_{4}\right), a\left(\tau_{2}, \tau_{3}, \tau_{4}\right)\right\} \\
\tau_{2} \rightarrow & \{b(\text { string })\} \\
\tau_{3} \rightarrow & \{c(\text { string })\} \\
\tau_{4} \rightarrow & \{d(\text { string })\}
\end{aligned}
$$

## Type inference for XML processing programs

- DTDs used as type declarations.


## Type inference for XML processing programs

- DTDs used as type declarations.
- Use of standard type checking for validation.


## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y)) .
$$

## Input DTD:

```
<!ELEMENT a (b,c)>
<!ELEMENT b (#PCDATA)>
<!ELEMENT c (#PCDATA)>
```


## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y))
$$

Input DTD:
<!ELEMENT a (b, c)>
<!ELEMENT b (\#PCDATA)>
<!ELEMENT c (\#PCDATA)>

Regular types:

$$
\begin{aligned}
\tau_{a} & \rightarrow\left\{a\left(\tau_{b}, \tau_{c}\right)\right\} \\
\tau_{b} & \rightarrow\{b(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\}
\end{aligned}
$$

## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y)) .
$$

Output DTD:

```
<!ELEMENT d (e,c)>
<!ELEMENT e (#PCDATA)>
<!ELEMENT c (#PCDATA)>
```


## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y))
$$

Output DTD:
<!ELEMENT d (e, c)>
<!ELEMENT e (\#PCDATA)>
<!ELEMENT c (\#PCDATA)>

$$
\begin{aligned}
\tau_{d} & \rightarrow\left\{d\left(\tau_{e}, \tau_{c}\right)\right\} \\
\tau_{e} & \rightarrow\{e(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\}
\end{aligned}
$$

## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y))::<\tau_{a}, \tau_{d}>
$$

$$
\begin{aligned}
\tau_{a} & \rightarrow\left\{a\left(\tau_{b}, \tau_{c}\right)\right\} \\
\tau_{b} & \rightarrow\{b(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\}
\end{aligned}
$$

## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y))::<\tau_{a}, \tau_{d}>
$$

$$
\begin{aligned}
\tau_{a} & \rightarrow\left\{a\left(\tau_{b}, \tau_{c}\right)\right\} \\
\tau_{b} & \rightarrow\{b(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\}
\end{aligned}
$$

$$
\begin{aligned}
\tau_{d} & \rightarrow\left\{d\left(\tau_{e}, \tau_{c}\right)\right\} \\
\tau_{e} & \rightarrow\{e(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\}
\end{aligned}
$$

## Type inference for XML processing programs

$$
\begin{aligned}
& p(a(X, Y), d(X, Y))::<\tau_{a}, \tau_{d}> \\
& \\
& \tau_{a} \rightarrow\left\{a\left(\tau_{b}, \tau_{c}\right)\right\} \\
& \tau_{b} \rightarrow\{b(\text { string })\} \\
& \tau_{c} \rightarrow\{c(\text { string })\}
\end{aligned}
$$

## Type inference for XML processing programs

$$
\begin{array}{rlrl}
p(a(X, Y), d(X, Y))::<\tau_{a}, \tau_{d} & > \\
& & \\
\tau_{a} \rightarrow\left\{a\left(\tau_{b}, \tau_{c}\right)\right\} \\
\tau_{b} & \rightarrow\{b(\operatorname{string})\} & & \\
\tau_{c} \rightarrow\{c(\operatorname{string})\} & \tau_{d} & \rightarrow & \left\{d\left(\tau_{e}, \tau_{c}\right)\right\} \\
& \tau_{e} & \rightarrow & \{e(\operatorname{string})\} \\
& \tau_{c} & \rightarrow & \{c(\operatorname{string})\}
\end{array}
$$

## Type inference for XML processing programs

$$
p(a(X, Y), d(X, Y))::<\tau_{a}, \tau_{d}>
$$

$$
\begin{aligned}
\tau_{a} & \rightarrow\left\{a\left(\tau_{b}, \tau_{c}\right)\right\} \\
\tau_{b} & \rightarrow\{b(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\} \\
\tau_{d} & \rightarrow\left\{d\left(\tau_{e}, \tau_{c}\right)\right\} \\
\tau_{e} & \rightarrow\{e(\text { string })\} \\
\tau_{c} & \rightarrow\{c(\text { string })\} \\
& \tau_{b} \cap \tau_{c}=\emptyset \Rightarrow \text { TYPE ERROR }
\end{aligned}
$$

## Type inference for XML processing programs

## Example:

If we want to translate the next document:
<catalogue>
<book>
<title> The Art of Computer Programming - Volume 1</title>
<author> D. Knuth </author>
<year> 1997 </year>
<publisher> Addison-Wesley </publisher> </book>
</catalogue>

## Type inference for XML processing programs

## Example:

Validated by the DTD:

```
<!ELEMENT catalogue (book)+>
<!ELEMENT book (title,author,year,publisher)>
<!ELEMENT title (#PCDATA)>
<!ELEMENT author (#PCDATA)>
<!ELEMENT year (#PCDATA)>
<!ELEMENT publisher (#PCDATA)>
```


## Type inference for XML processing programs

## Example:

To this new document:
<catalogue>
<book>
<title> The Art of Computer Programming - Volume $1</$ title> <year> 1997 </year>
</book>
</catalogue>

## Type inference for XML processing programs

## Example:

Validated by the DTD:

> <!ELEMENT catalogue (book)+>
> <!ELEMENT book (title,year)>
> <!ELEMENT title (\#PCDATA)>
> <!ELEMENT year (\#PCDATA)>

## Type inference for XML processing programs

## Example:

The next (simple) program is enough:
process (catalogue(L1), catalogue(L2)) :conversion(L1,L2).
conversion([book $(A,-, Z,-)],[\operatorname{book}(A, Z)])$.
conversion([book(A, _ , Z, _)|R1], [book(A, Z)|R2]):conversion(R1,R2).

## Conclusions

Relation between Regular Types and DTDs.

## Conclusions

- Relation between Regular Types and DTDs.
- Translating XML documents to Prolog terms.


## Conclusions

- Relation between Regular Types and DTDs.
- Translating XML documents to Prolog terms.
- Type checking leads to correct processing of XML.


## Future work

- Improve the efficiency of the type inference algorithm.


## Future work

- Improve the efficiency of the type inference algorithm.
- "Real-world" applications.


## END

